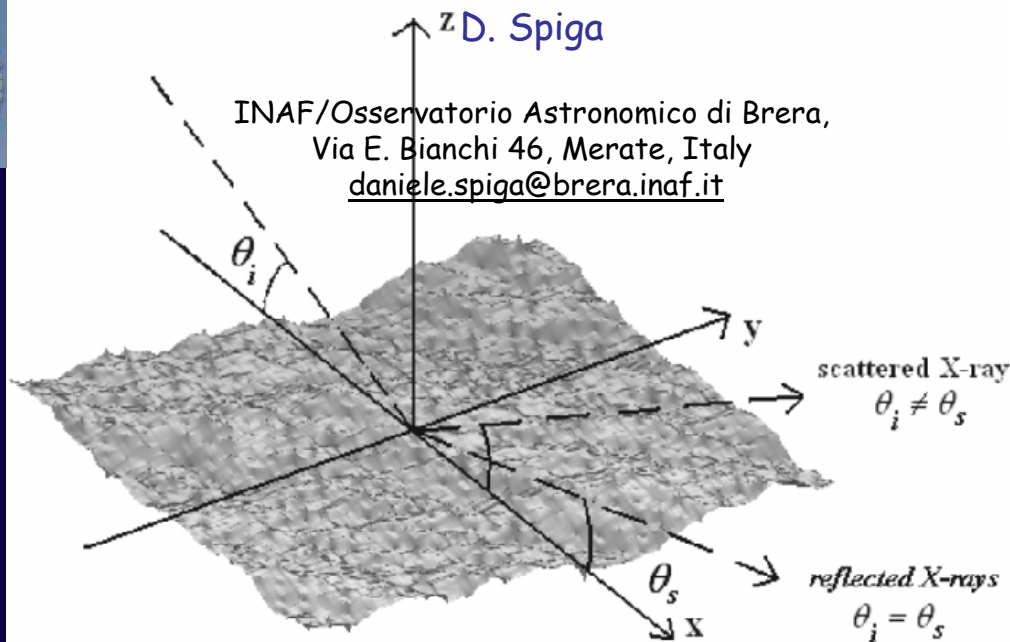


# X-ray imaging telescopes: prediction of the expected image quality from surface roughness metrology data



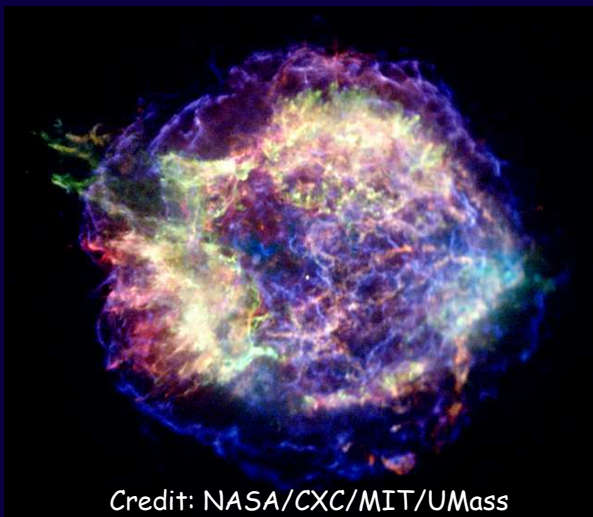
INAF/Osservatorio Astronomico di Brera,  
Via E. Bianchi 46, Merate, Italy  
[daniele.spiga@brera.inaf.it](mailto:daniele.spiga@brera.inaf.it)

This work is supported by ASI (the Italian Space Agency)

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## WHAT X-RAY ASTRONOMERS WANT: HIGH ANGULAR RESOLUTION...



Credit: NASA/CXC/MIT/UMass  
Amherst/M.D.Stage et al.



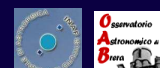
Credit: NASA/Swift-XRT

Chandra image, res. = 0.5 arcsec HEW

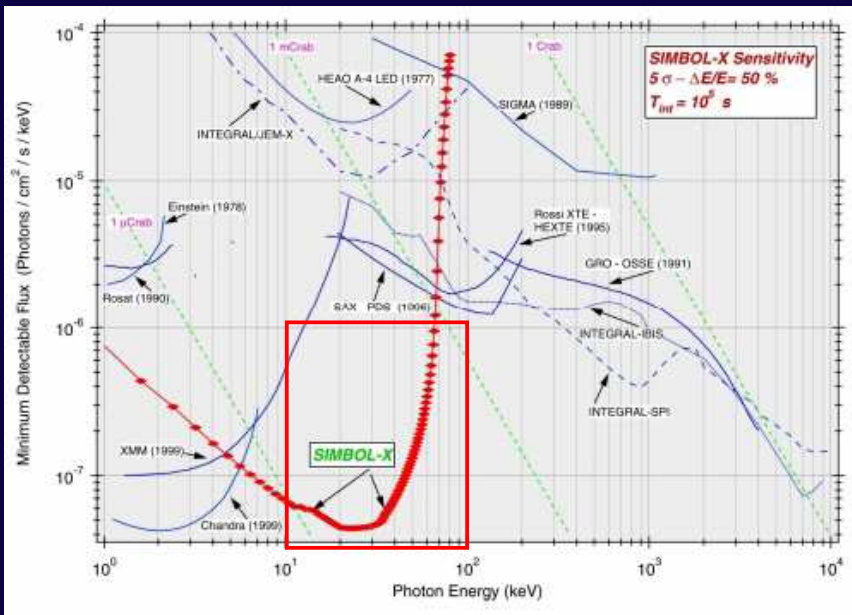
Swift XRT image, res. = 15 arcsec HEW

The angular resolution of X-ray telescopes is a fundamental requirement to resolve the details of celestial sources

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## ... AND LARGE EFFECTIVE AREAS



- Most X-ray sources are faint, large collecting areas ( $\sim 1000 \text{ cm}^2$ ) are needed to increase the sensitivity.

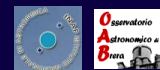
- A limited mass ( $\sim 300 \text{ kg}$ ) for the telescope to fly...!

- High stability in orbital environment (variations of temperature, cosmic rays, micrometeoroids, ...)

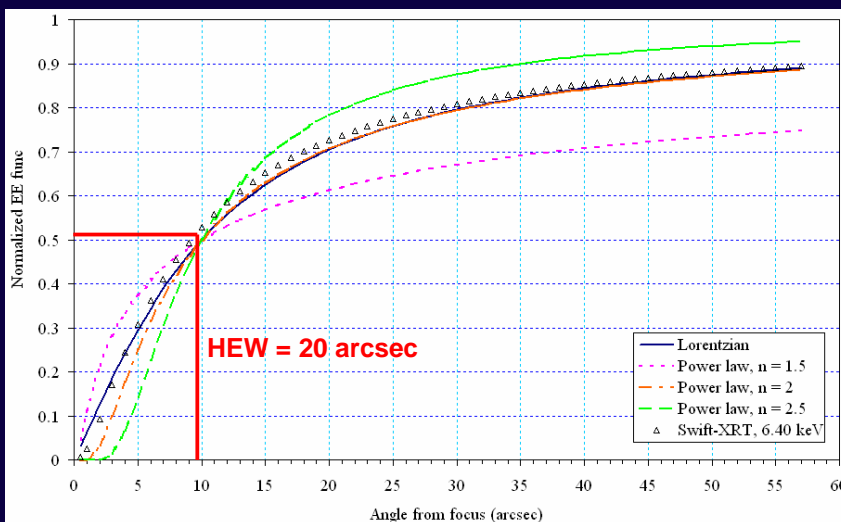
X-ray telescopes must have the capability to detect *extremely weak fluxes* (down to  $10^{-8} \text{ ph/s/cm}^2/\text{keV}$ ).

To date, the energy range 10 - 100 keV has still to be explored with *direct imaging* telescopes.

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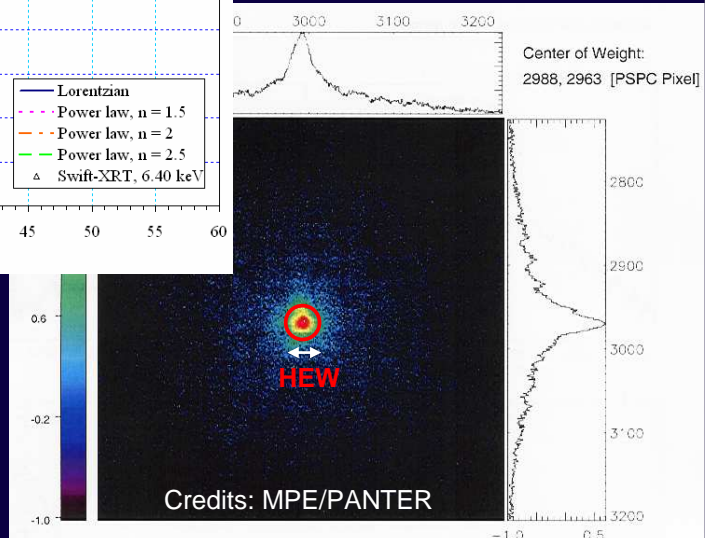


## ASTRONOMERS LIKE USING THE HEW (= Half Energy Width)



HEW (or HPD, Half Power Diameter) = the angular diameter in arcsec including 50% of focused photons

Other parameters (like FWHM) would be, in general, non-representative of the optical performances (exception: nearby sources)

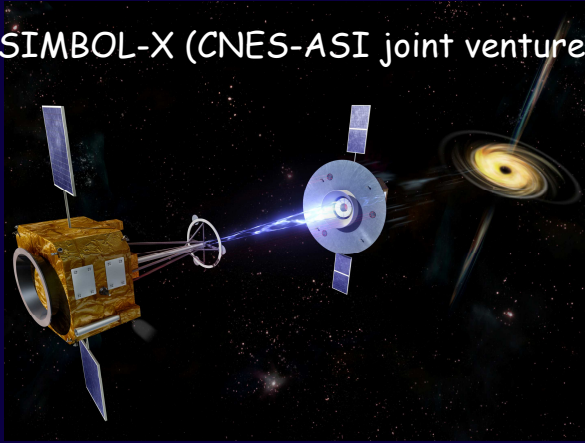


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## A NEW HARD X-RAY MISSION

### SIMBOL-X (CNES-ASI joint venture)



Focal length	20 m
Min diameter	300 mm
Max diameter	700 mm
Min incidence angle	0.11 deg
Max incidence angle	0.25 deg
Energy band	0.5 – 80 keV
Number of shells	100
Effective area (1 keV)	~ 1400 cm <sup>2</sup>
Effect. area (30 keV)	~ 450 cm <sup>2</sup>
Field of View	12 arcmin
Required HEW	15 arcsec (1 keV) 20 arcsec (40 keV)

SIMBOL-X will allow the extension of imaging capabilities to the hard X-ray band by adopting:

- Very shallow incidence angles (0.1-0.25 deg), made possible by a 20 m focal length, managed with the **formation flight** configuration.
- Graded **multilayer coatings** to enhance mirrors' reflectivity up to 80 keV

G. Pareschi, P. Ferrando, "The SIMBOL-X hard X-ray mission", Exp. Astron. 20, 139-149 (2006)

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## CONTRIBUTIONS TO IMAGING DEGRADATION

1) An energy-independent term  $H_0$ , caused by the

a) **single mirror figure errors**

b) alignment of mirrors

Ray tracing from profiles,  
UV bench measurement

2) An energy-dependent term  $H(\lambda)$ , caused by  
surface roughness X-ray scattering (XRS)

Physical optics

$$HEW^2(\lambda) \approx H_0^2 + H^2(\lambda)$$

Correction  
with active  
optics

not effective if this term prevails (in hard X-rays)

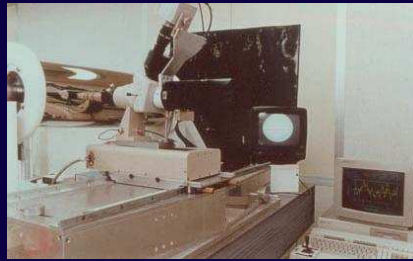
Accurate roughness metrology urge!



# METROLOGICAL INSTRUMENTATION FOR MIRROR DIAGNOSTIC AT INAF-OAB



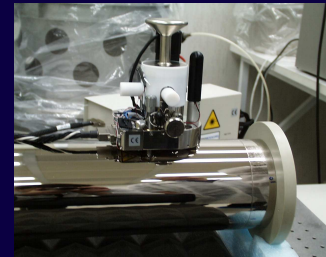
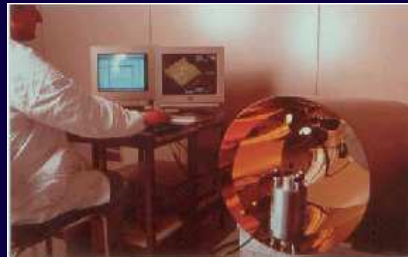
Long-Trace profilometer - suitable for stress-induced deformations



WYKO profilometer  
1D surface profiles  
2.5, 0.6 mm wide scans



Nomarski Phase Contrast microscope  
5x - 100x



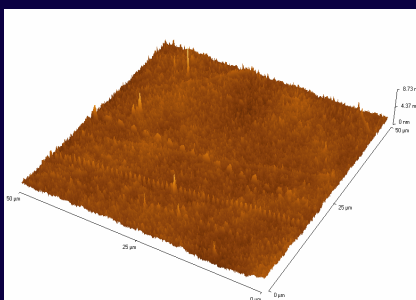
2 Atomic Force Microscopes  
2D surface maps (plane and curved substrates): 100, 101  $\mu\text{m}$  wide scans

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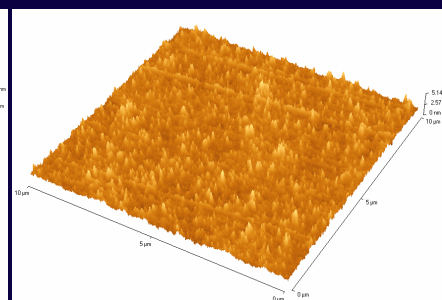


## X-RAY MIRROR SURFACE ROUGHNESS MEASUREMENTS

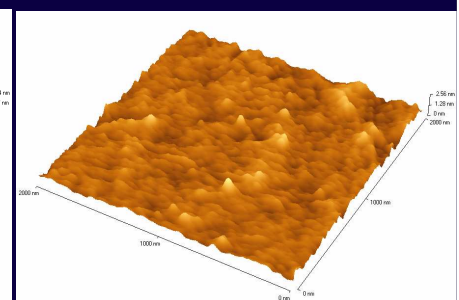
- Each instrument is sensitive only to a particular window of spatial frequencies.



AFM, 100  $\mu\text{m}$  - 0.4  $\mu\text{m}$   
 $\sigma = 2.9 \text{ \AA}$

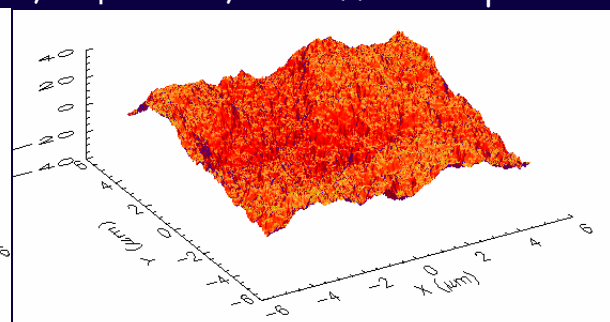
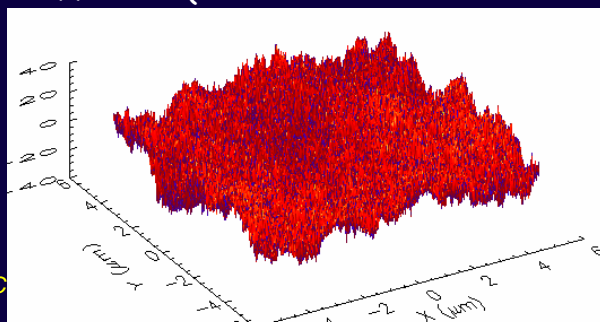


AFM, 10  $\mu\text{m}$  - 40 nm  
 $\sigma = 2.6 \text{ \AA}$



AFM, 1  $\mu\text{m}$  - 4 nm  
 $\sigma = 1.4 \text{ \AA}$

- Also in the same bandwidth, surfaces with the same rms can be VERY different (see below: same rms = 10  $\text{\AA}$ , 10  $\mu\text{m}$  wide, but different spectrum)



## REPRESENTATION IN TERMS OF POWER-SPECTRAL DENSITY

Representing the roughness in terms of PSD (Power-Spectral-Density) has several advantages (and at least a disadvantage):

$$P(f) = \frac{1}{L} \left| \int_0^L z(x) e^{-2\pi i f x} dx \right|^2$$

height

$$\sigma_{\Delta f}^2 = \int_{\Delta f} P(f) df$$

slope

$$m_{\Delta f}^2 = \int_{\Delta f} (2\pi f)^2 P(f) df$$

curvature

$$c_{\Delta f}^2 = \int_{\Delta f} (2\pi f)^4 P(f) df$$

- ☺ PSDs from different instruments are (in general) mutually-consistent
- ☺ PSDs in the same bandwidth can be averaged to reduce sampling effects
- ☺ The PSD returns a complete description of the statistical properties of roughness
- ☺ It directly involves the X-ray scattering and, therefore, the image degradation!
- ☹ It provides little or no information for ray-tracing...

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## DIRECT DERIVATION OF THE $H(\lambda)$ FROM A SURFACE PSD

PSD  $\longrightarrow$   $H(\lambda)$

Spiga D., 2007, "Analytical evaluation of the X-ray scattering contribution to imaging degradation in grazing-incidence X-ray telescopes". *Astronomy and Astrophysics*, vol. 468, 775-784

$$\int_{f_0}^{2/\lambda} P(f) df = \frac{\lambda^2}{16\pi^2 \sin^2 \vartheta_i} \ln\left(\frac{2N}{2N-1}\right)$$

$\rightarrow$  derive  $f_0 \rightarrow$

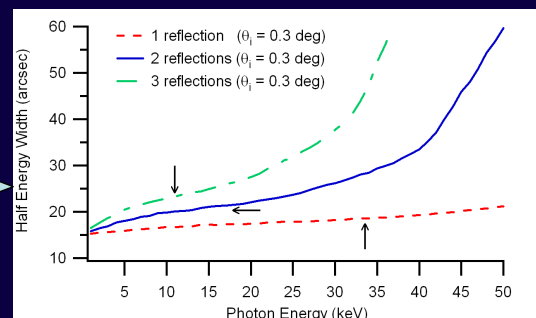
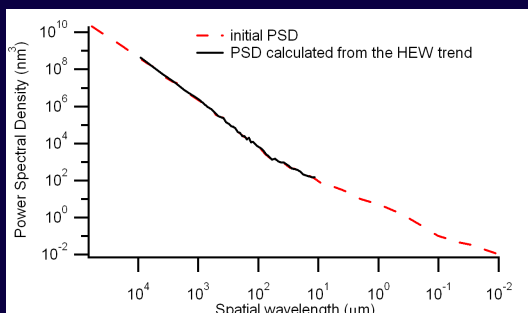
$$H(\lambda) = \frac{2\lambda f_0}{\sin \vartheta_i}$$

$N$  : number of identical reflections

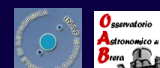
$\vartheta_i$  : grazing incidence angle

$\lambda$  : photon wavelength

$f$  : surface spatial frequency



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## DIRECT DERIVATION OF THE $H(\lambda)$ FROM A SURFACE PSD

### For a fractal surface

Spiga D., 2007, "Analytical evaluation of the X-ray scattering contribution to imaging degradation ingrazing-incidence X-ray telescopes". Astronomy and Astrophysics, vol. 468, 775-784

$$P(f) = \frac{K_n}{f^n}$$

1 reflection

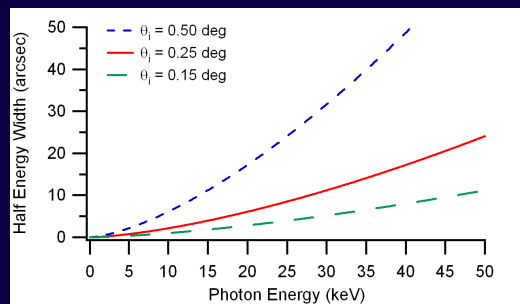
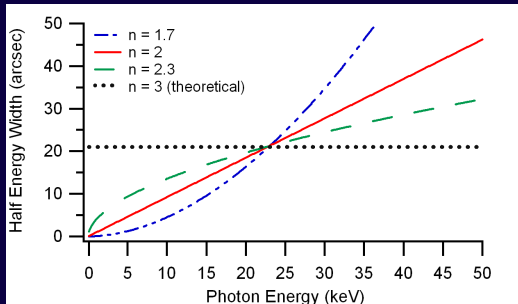
$$H(\lambda) = 2 \left[ \frac{16\pi^2 K_n}{(n-1)\ln 2} \right]^{\frac{1}{n-1}} \left( \frac{\sin \vartheta_i}{\lambda} \right)^{\frac{3-n}{n-1}}$$

The  $H(\lambda)$  function is also a **power-law**, with a spectral index

$$\gamma = \frac{3-n}{n-1}$$

1)  $\gamma > 0$ , because fractal **surfaces** have  $1 < n < 3$  !!!

2) For a fixed  $K_n$ : the steeper the PSD, the better!!



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## DIRECT DERIVATION OF THE PSD FROM A $H(\lambda)$ FUNCTION

PSD  $\rightarrow$   $H(\lambda)$

Spiga D., 2007, "Analytical evaluation of the X-ray scattering contribution to imaging degradation ingrazing-incidence X-ray telescopes". Astronomy and Astrophysics, vol. 468, 775-784

$$\frac{P(f_0)}{\lambda} \frac{d}{d\lambda} \left( \frac{H(\lambda)}{\lambda} \right) + \frac{1}{4\pi^2 \sin^3 \vartheta_i} \ln \left( \frac{2N}{2N-1} \right) \approx 0$$

At the frequency

$$f_0 = \frac{H(\lambda)}{2\lambda} \sin \vartheta_i$$

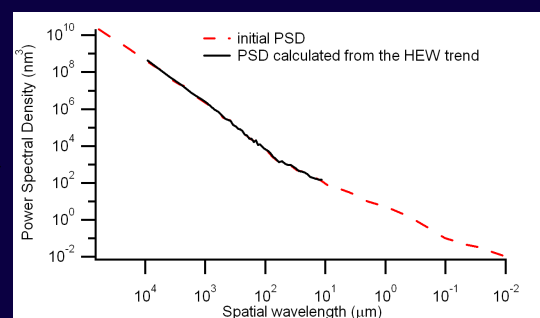
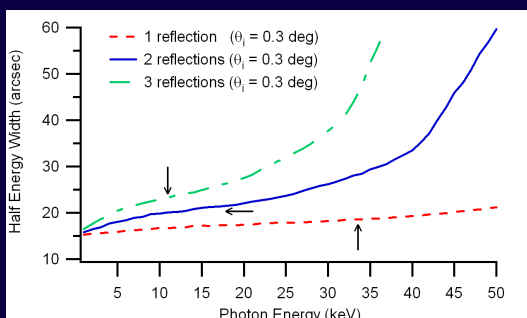
$N$ : number of identical reflections

$\lambda$ : photon wavelength

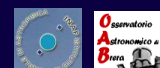
$\vartheta_i$ : grazing incidence angle

$f$ : surface spatial frequency

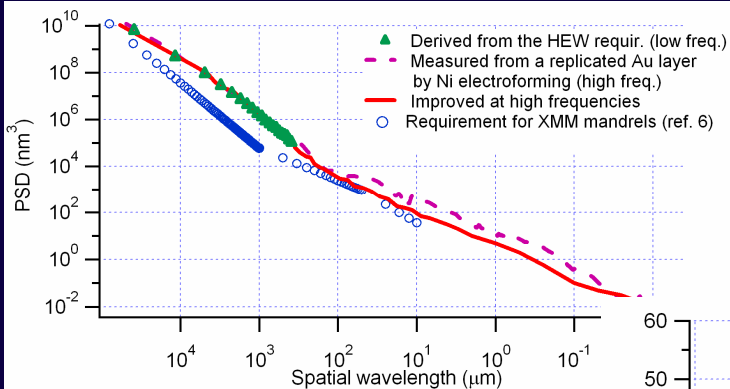
These formulae can be useful to translate HEW requirements into PSD tolerances !!!!



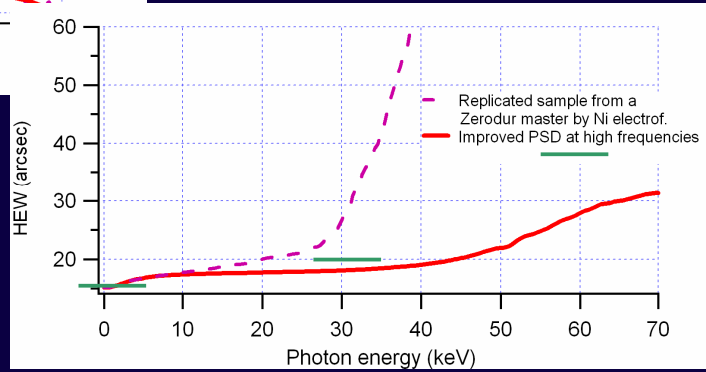
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## ROUGHNESS TOLERANCES FOR SIMBOL-X



( $H_0 = 15$  arcsec)



D. Spiga, G. Pareschi, R. Canestrari, and V. Cotroneo, "Estimation of the X-ray scattering impact in imaging degradation for the SIMBOL-X Telescope", Mem. S.A.It. Vol. 79, 278

PSD	$1 \text{ mm} > \ell > 100 \text{ } \mu\text{m}$	$100 \text{ } \mu\text{m} > \ell > 10 \text{ } \mu\text{m}$	$10 \text{ } \mu\text{m} > \ell > 1 \text{ } \mu\text{m}$	$\ell < 1 \text{ } \mu\text{m}$
violet	$10.2 \text{ \AA}$	$3.6 \text{ \AA}$	$2.5 \text{ \AA}$	$1.8 \text{ \AA}$
red	$9.3 \text{ \AA}$	$2.2 \text{ \AA}$	$1.3 \text{ \AA}$	$1.0 \text{ \AA}$

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## FINAL REMARKS

- Active optics for X-rays can correct the mirror profiles, but what if X-ray scattering due to roughness degrades the image?
- X-ray scattering seems to pose the main threat to the telescope angular resolution. Clear roughness tolerances should be established from **scientific requirements** of the telescope.
- Treatment of roughness in terms of PSD allows to relate it PSD to the expected HEW trend, as a function of  $\lambda$  (and vice versa).
- Application of simple formulae allows determining the surface finishing tolerances for focusing mirrors in soft and hard X-rays.

## FUTURE WORK

- Extending the formalism to any multilayer coating.
- Apply the method to explain the angular resolution of existing X-ray telescopes like Swift/Jet-X.

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