

# ORBITAL SELECTIVITY AND HUND'S PHYSICS IN IRON-BASED SC

Laura Fanfarillo



# FROM FERMIL LIQUID TO NON-FERMIL LIQUID

Strong  
Correlation



Low  
Temperature



High  
Temperature

Fermi  
Liquid



Tuning parameter

# FROM FERMIL LIQUID TO NON-FERMIL LIQUID

Strong  
Correlation



Low  
Temperature



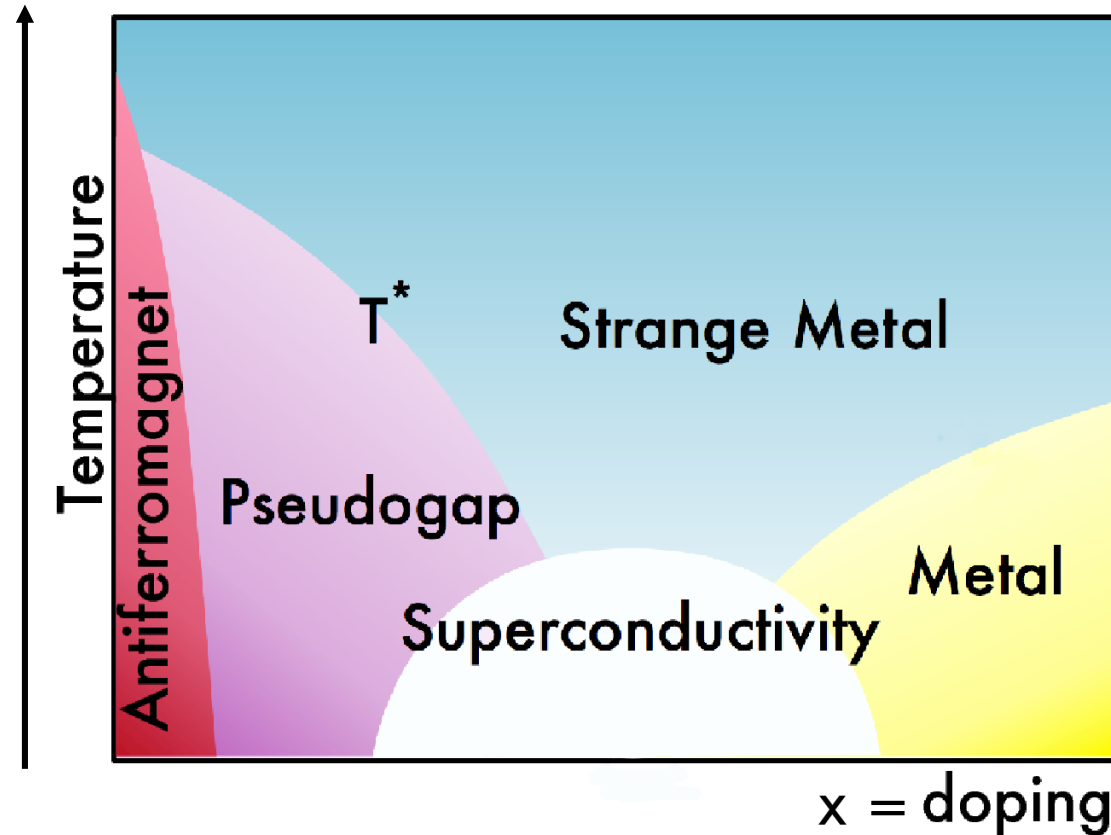
High  
Temperature

Fermi  
Liquid



Unconventional SC emerges at low temperature from a state that is far from an ideal metal

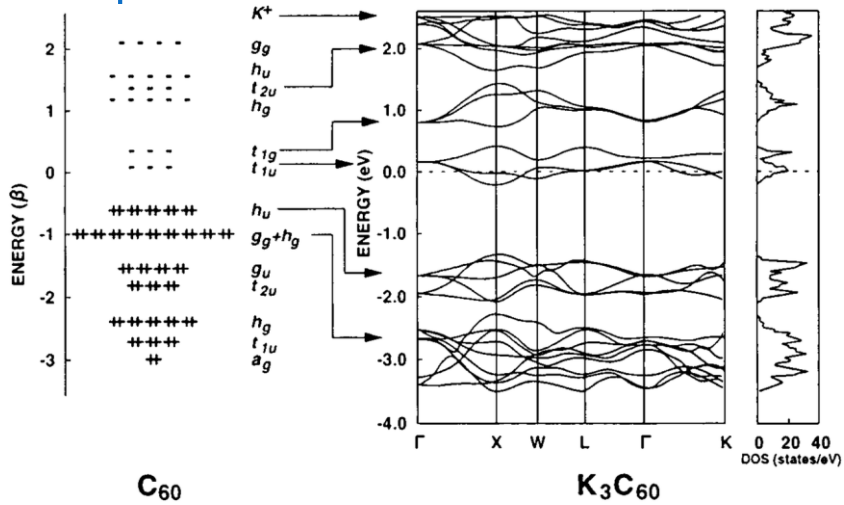
# FROM FERMI LIQUID TO NON-FERM LIQUID : CUPRATES



Physics of a doped  
Mott Insulator

Unconventional SC emerges at low temperature from a state that is  
far from an ideal metal

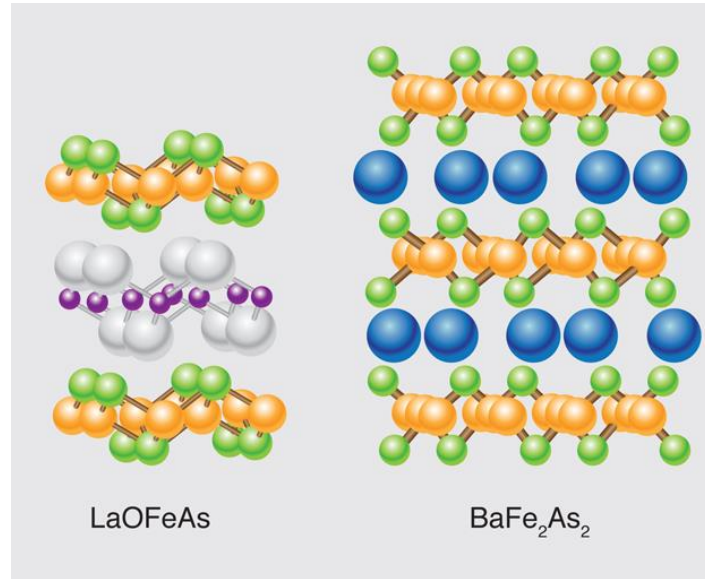
# MULTIORBITAL PHYSICS IN CORRELATED SYSTEMS



$C_{60}$

$K_3C_{60}$

Ruthenates, Iridates ...

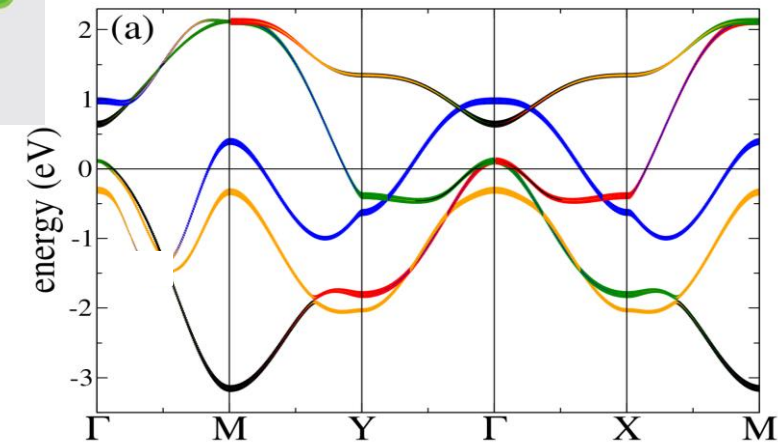
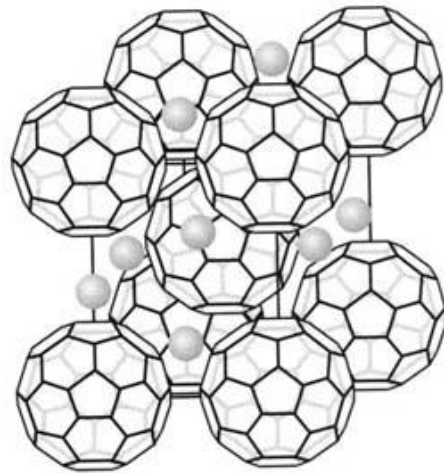


LaOFeAs

BaFe<sub>2</sub>As<sub>2</sub>

... and  
Iron based SC

$A_3C_{60}$   
Mitrano, Kim  
& Nomura talks



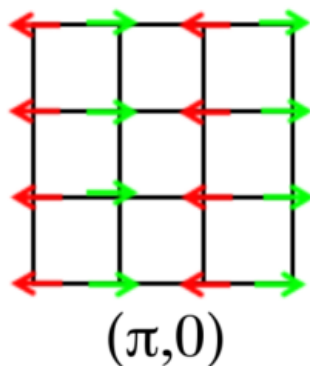
# UNCONVENTIONAL SC & BAD METAL PHASE

Unconventional SC emerges at low temperature from a state that is far from an ideal metal

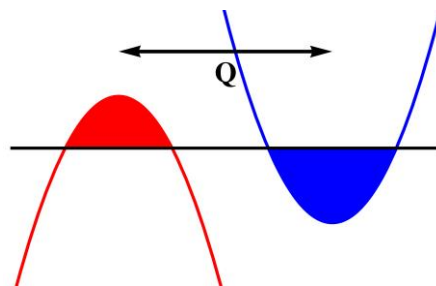
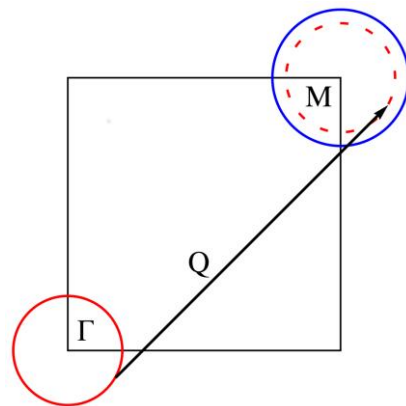
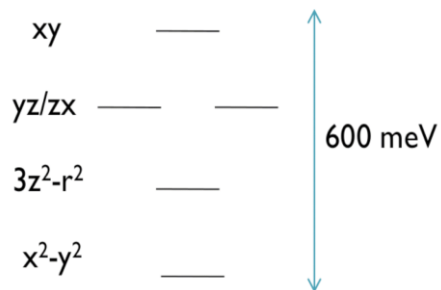
**How multiorbital physics affect this picture?**

# THE IRON AGE OF SC

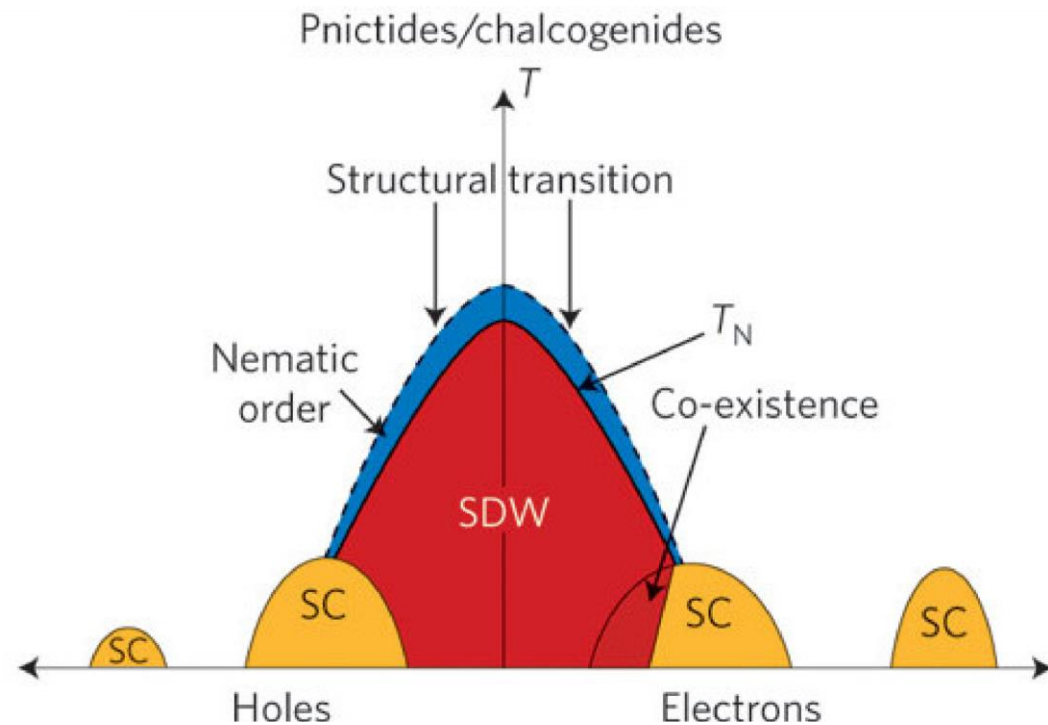
Parent Compound:  
SDW bad metal



Multiband SC System:  
3d Iron orbitals



Q - SDW vector



Nodless gap:  $s_{\pm}$   
symmetry

# IRON-BASED MATERIALS: CORRELATED OR NOT?

## Contrasting evidences for correlation strength

weak

- no Mott insulator in the phase diagram
- hard detection of any Hubbard bands
- moderate correlations from Optics

- Strong mass renormalization from ARPES, Q. Osc. with respect DFT
- bad metallicity
- strong sensitivity to doping

strong

Itinerant electron vs Localized electrons picture



# IRON-BASED MATERIALS: INTERMEDIATE CORRELATED MATERIAL?

Strong  
Correlation



Orbital Selective Mott  
physics:

Small Crystal Field Splitting +  
Hund's coupling

Fermi  
Liquid



Localized Electrons Picture

Magnetic SuperExchange

Itinerant Electrons Picture

Fermi-Surface Instabilities  
(Nesting)

DeMedici et al PRL 107 2011,  
DeMedici et al, PRL 112 2014,  
Fanfarillo et al PRB 92 2015 ...

# MOTT-HUBBARD INSULATOR: SINGLE ORBITAL CASE HALF FILLING

Despite the conduction band is half-filled the system is insulating because of the strong Coulomb repulsion

Quasiparticle Spectral Weight Suppressed

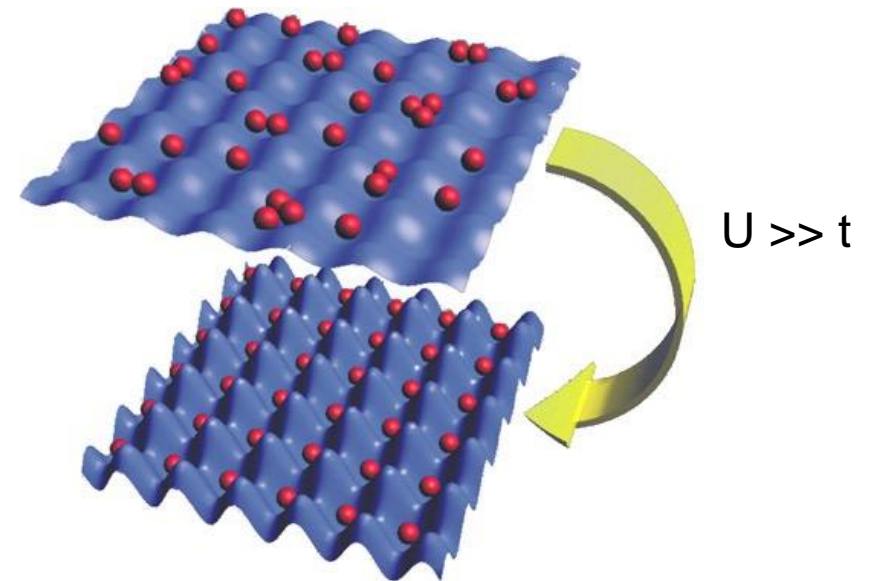
$Z \sim 1/m^*$  increasing of correlation

Charge Fluctuations Suppressed:

localization of the electrons

Spin Fluctuations Enhanced

atoms are locally spin polarized

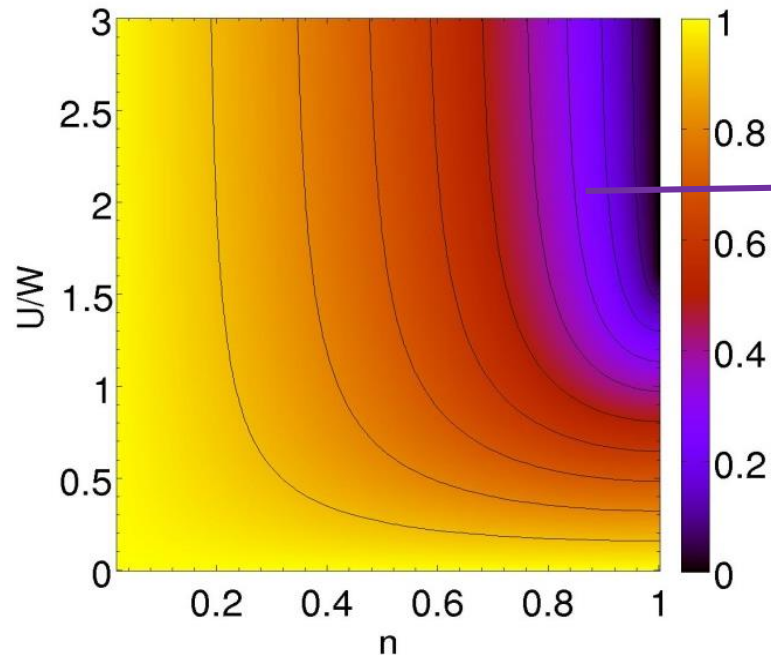


$Z=1$  FL - Metal

$Z=0$  Correlated electrons - Insulator

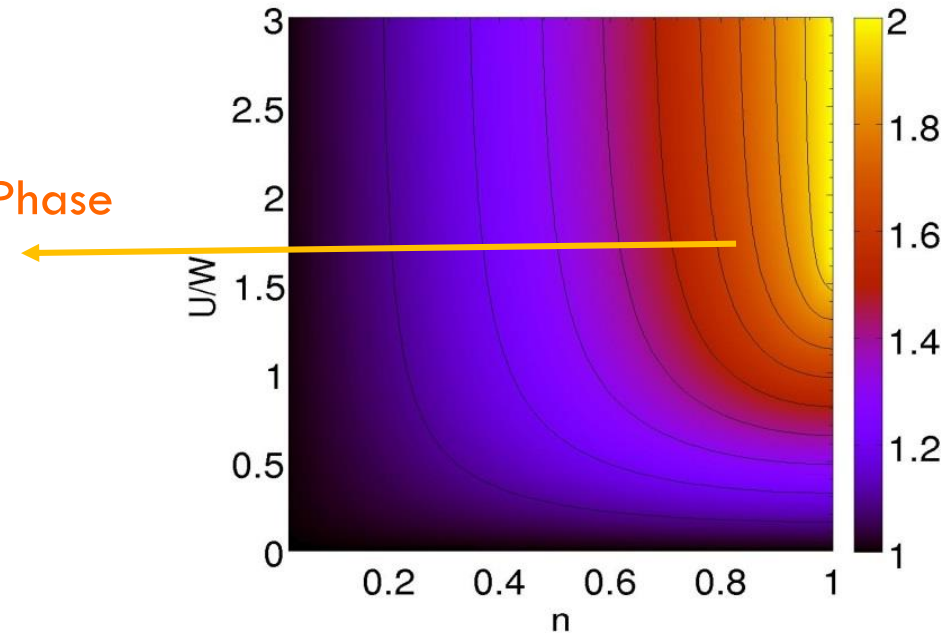
# MOTT-HUBBARD INSULATOR: SINGLE ORBITAL CASE IN DOPING

Far from half-filling ( $n \neq 1$ ):



Correlated bad metal close to the Mott insulator

High Spin Phase



# MULTIORBITAL MODEL: U, JH

$$\begin{aligned}
 H = & \sum_{i,j,\gamma,\beta,\sigma} t_{i,j}^{\gamma,\beta} c_{i,\gamma,\sigma}^\dagger c_{j,\beta,\sigma} + h.c. + U \sum_{j,\gamma} n_{j,\gamma,\uparrow} n_{j,\gamma,\downarrow} \\
 & + (U' - \frac{J_H}{2}) \sum_{j,\gamma > \beta,\sigma,\tilde{\sigma}} n_{j,\gamma,\sigma} n_{j,\beta,\tilde{\sigma}} - 2J_H \sum_{j,\gamma > \beta} \vec{S}_{j,\gamma} \vec{S}_{j,\beta} \\
 & + J' \sum_{j,\gamma \neq \beta} c_{j,\gamma,\uparrow}^\dagger c_{j,\gamma,\downarrow}^\dagger c_{j,\beta,\downarrow} c_{j,\beta,\uparrow} + \sum_{j,\gamma,\sigma} \epsilon_\gamma n_{j,\gamma,\sigma} .
 \end{aligned}$$

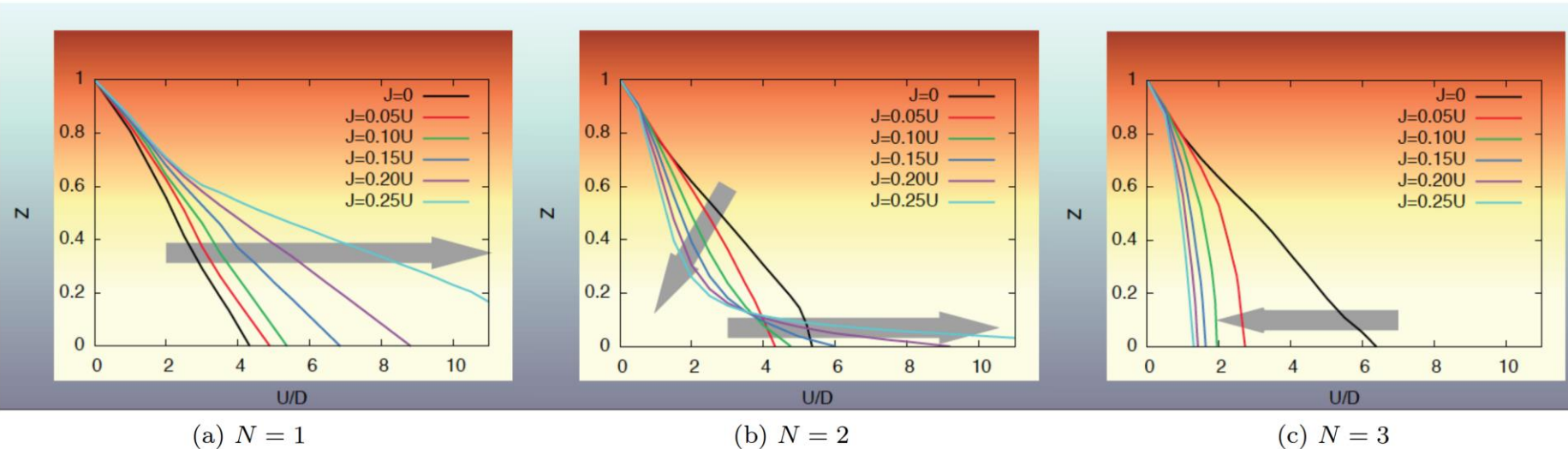
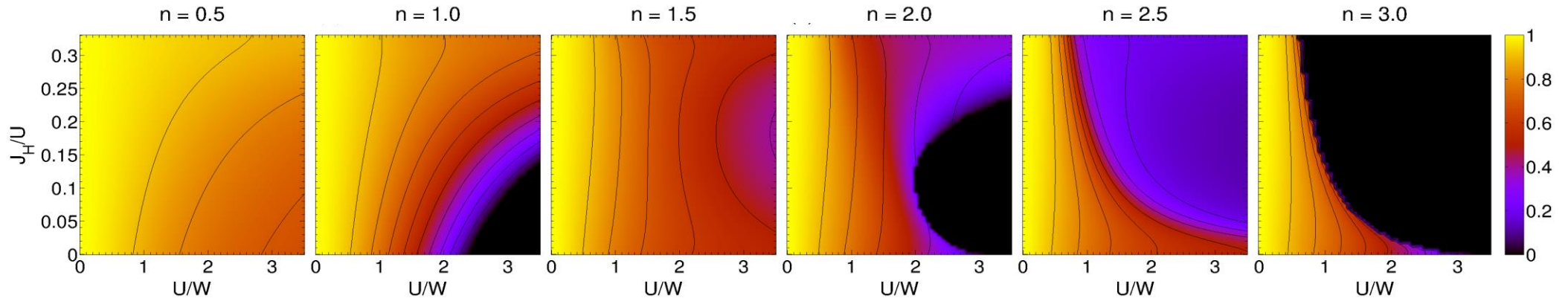
tb (hopping term)                      Intra-orbital repulsion  
Inter-orbital repulsion                      Hund's coupling  
Pair hopping

Interactions are local and satisfy rotational invariance:  $U' = U - 2J_H$

$U$  and  $J_H$  are free parameters

# MORE IS DIFFERENT: 3 ORBITALS

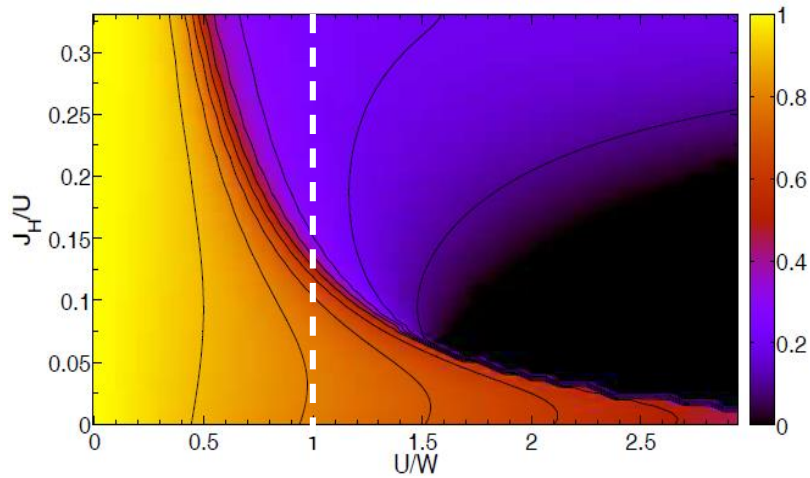
Quasiparticle  
Spectral Weight  
 $Z(U, J_H)$



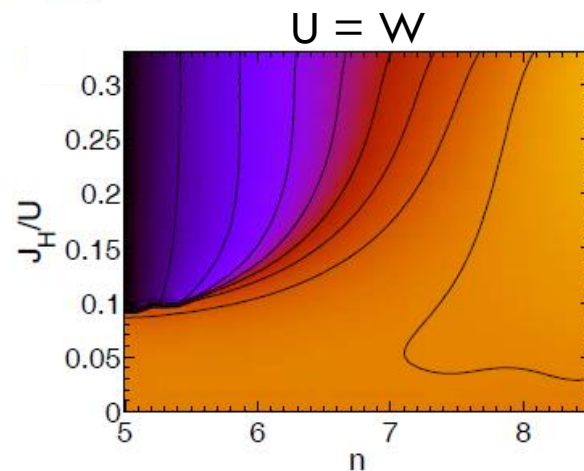
- Bad metals close to HF Mott Insulator
- Hund's metal boundary follows the MI transition line
- 2(4) el/3orb Hund induces correlated metal state

# THE IBS CASE: 6 ELECTRONS IN 5 ORBITALS

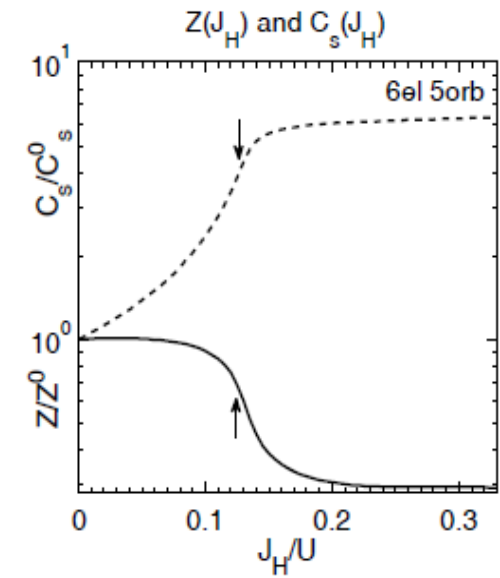
6 el in 5 orb



Hund'metal linked to the half-filled  $n=5$  Mott insulator  
*doping asymmetry around  $n=6$*

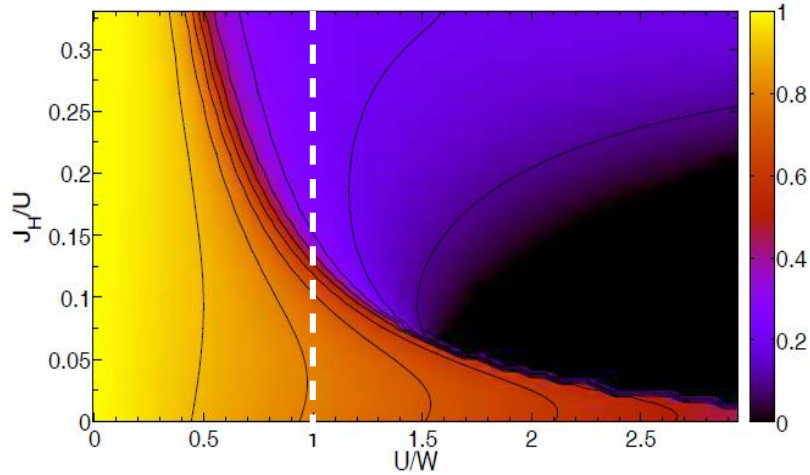


Hund's coupling induced high spin configuration

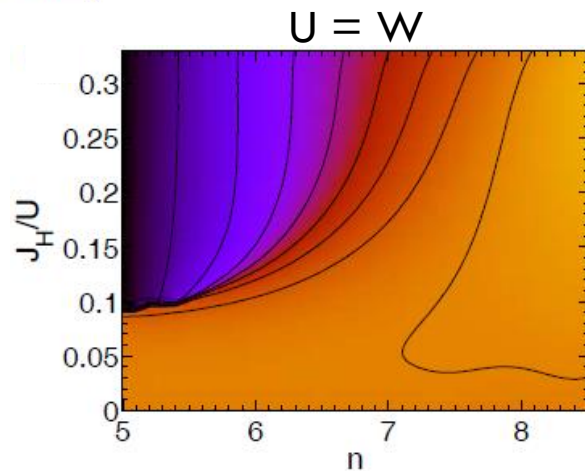


# THE IBS CASE: 6 ELECTRONS IN 5 ORBITALS

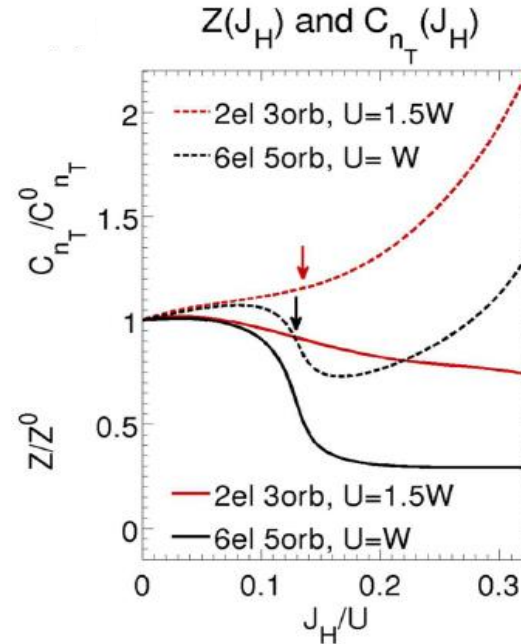
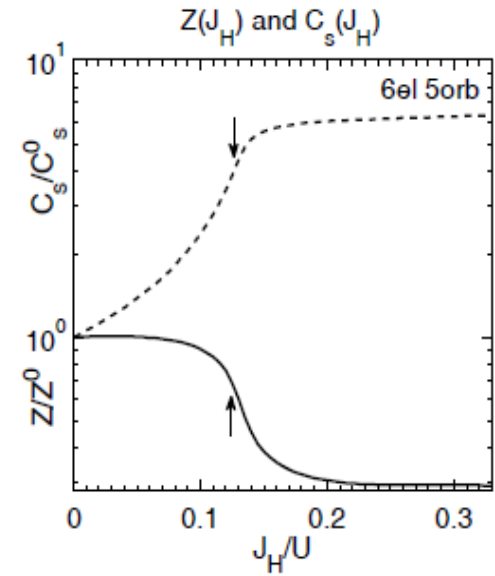
6 el in 5 orb



Hund'metal linked to the half-filled  $n=5$  Mott insulator *doping asymmetry around  $n=6$*



Hund's coupling induced high spin configuration



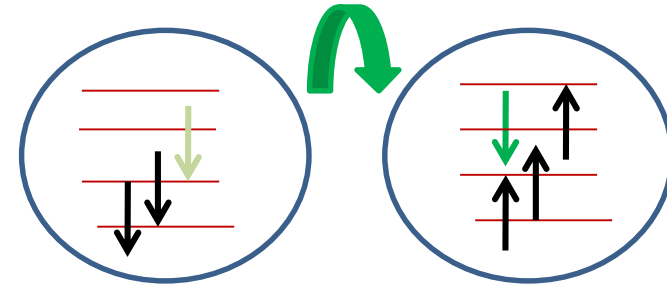
Quasiparticle weight and charge fluctuations:

Correlation vs Localization



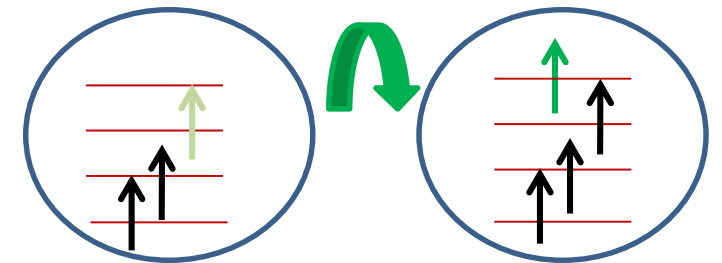
# HUND'S METAL: LINK TO HF MOTT TRANSITION

- ❑ Suppression of coherence due to suppression of hopping processes which involve **intraorbital double occupancy**



$$E^{intra\uparrow\downarrow} = U + (n - 1)J_H$$

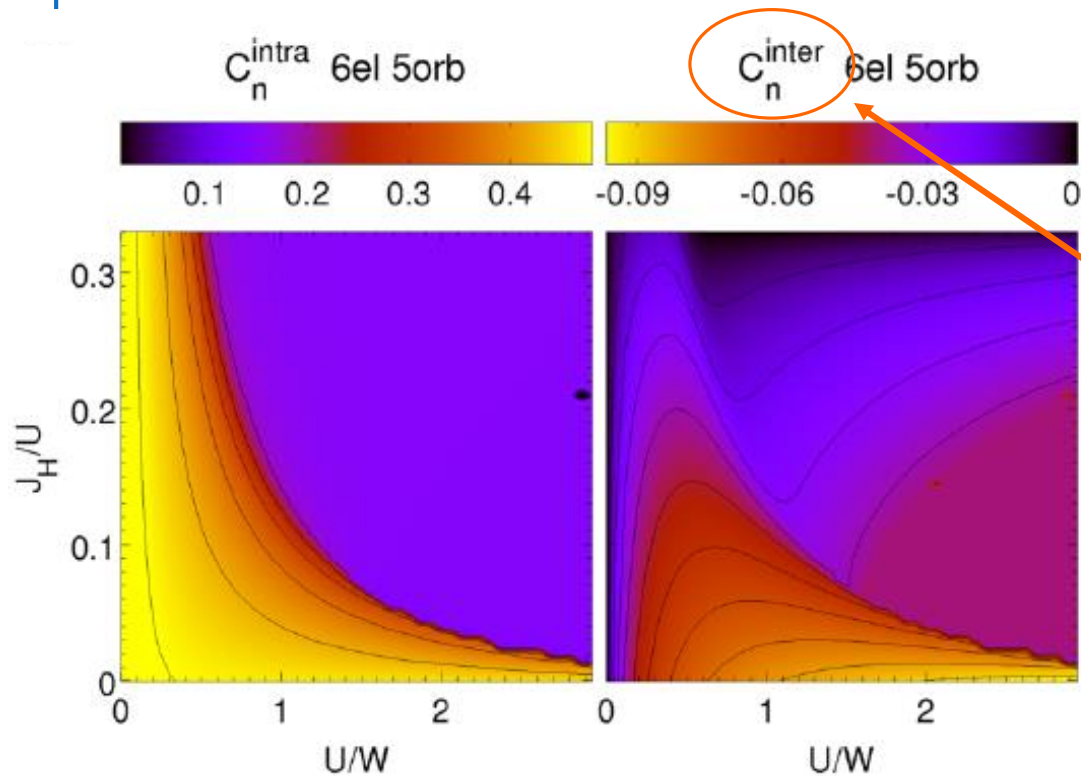
- ❑ Enhancement of charge fluctuations due to hopping processes which involve parallel spins to an empty orbital



$$E^{\uparrow\uparrow} = U - 3J_H$$



# HUND'S METAL: LINK TO HF MOTT TRANSITION



As the double occupancies are suppressed:

- atoms becomes *spin polarized*

- *orbitals decoupled*

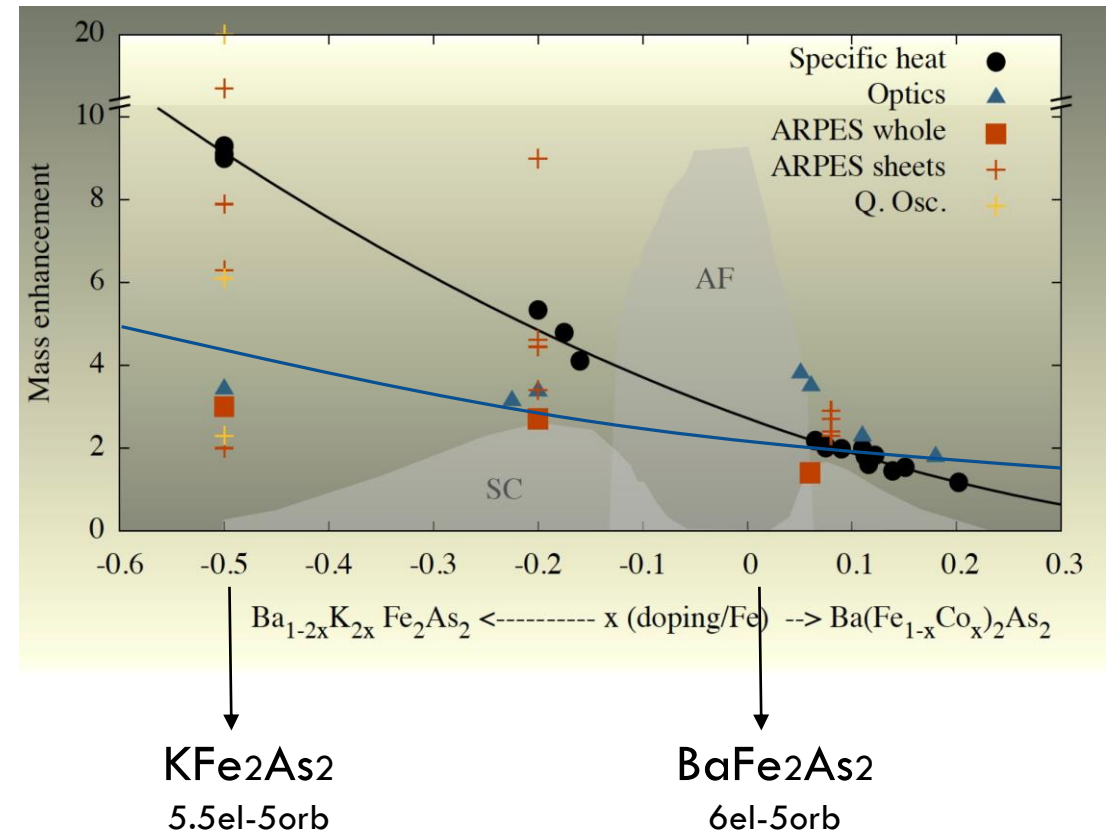
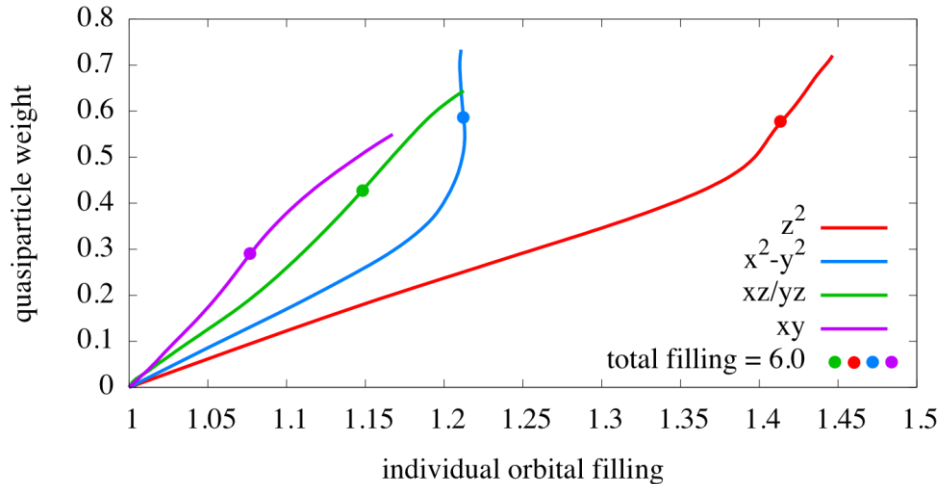
In the polarized state the effective interorbital interaction between the electrons decreases.

It vanishes at  $J_H = U/3$ .

# HUND'S PHYSICS IN IBS: EFFECTIVE MASS

- $m^*$  increases reducing the # of electrons
- $m^*$  strongly orbital selective

BaFe<sub>2</sub>As<sub>2</sub> - total filling from 6.25 to 5.0



- Each orbital has a different  $Z_\alpha \sim 1/m_\alpha^*$  proportional to the orbital filling

***Each orbital behaves as a doped Mott insulator***

# CONCLUSIONS: HUND'S PHYSICS IN IBS

- More is different:
  - Correlation is **not** a good measure of localization
  - The degree of correlation is **complicated by the multiorbital physics**
- IBS (parent compound 6 el/5 orb)
  - ***IBS collection of five decoupled single-band doped Mott insulator***
    - $n = 6$  is not a special point for correlations:
  - **Correlations increase reducing the number of electrons in d-bands:**
    - $\text{KFe}_2\text{As}_2$  is much more correlated than  $\text{BaFe}_2\text{As}_2$

# CAN WE GO FURTHER?

## ORBITAL SELECTIVITY AND HUND'S PHYSICS IN THE PHASE DIAGRAM OF IBS

- *From the strong correlated side*

Try to figure out if local correlations can explain the phase diagram of IBS  
Orbital selective SC ...

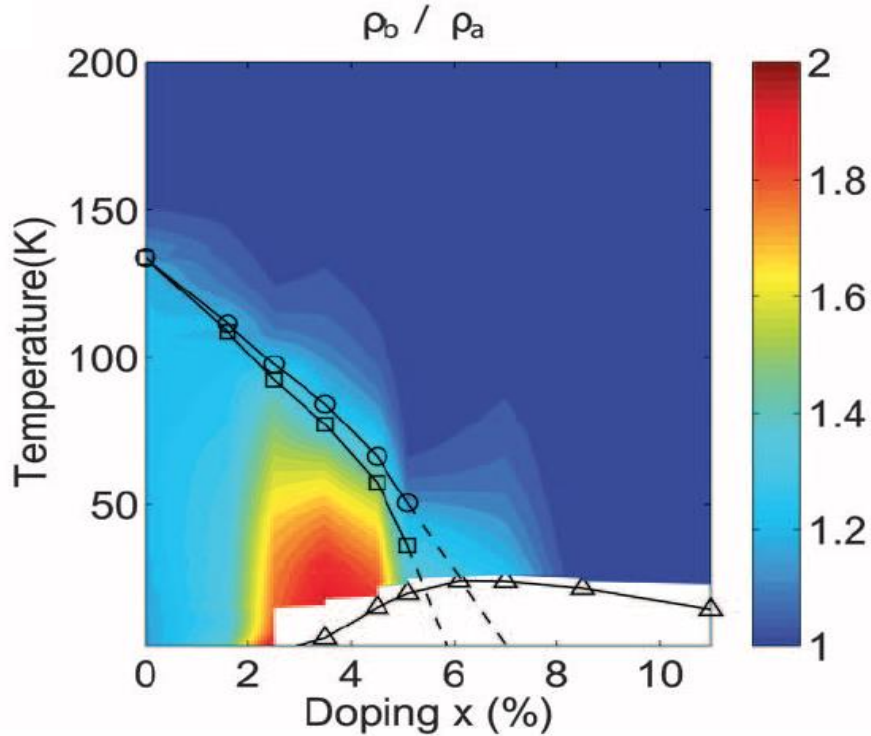
Fanfarillo et al arXiv 1609.06672

- *From the FL side*

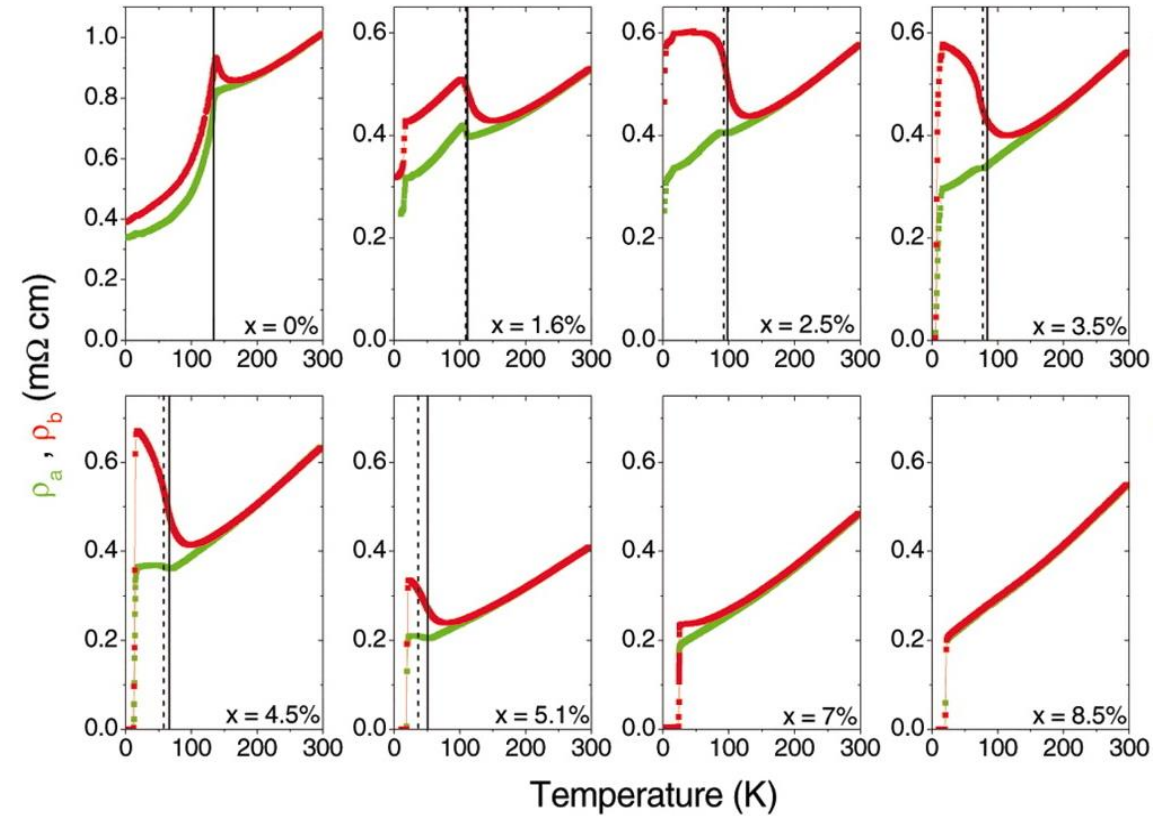
Project interacting multiorbital Hamiltonian into low-energy model for IBS  
Orbital selective character of spin fluctuations  
(SC orbital selective glue)

Fanfarillo et al. PRB 91 (2015),  
Christenses et al. PRB 93 (2016)  
Fanfarillo et al arXiv 1605.02482 ...

# NEMATIC PHASE OF IBS



## Resistivity anisotropy measurements



J-H Chu et al. Science 329 (2010)

Structural transition takes place before/simultaneously to the magnetic one:

Several experimental probes revealed  $x,y$  anisotropy above the magnetic transition not only in the lattice parameter but also in the electronic properties: [NEMATIC PHASE](#)

# MATTER OF ANISOTROPY

Possible origin of “nematic phase”:

- Structural distortion → Anisotropy from the lattice parameters (odd!)
- Orbital/Charge order → Anisotropy from the orbital filling
- Spin order → Anisotropy from spin fluctuations along  $x,y$

Classical “*chicken and egg problem*”

All three types of order (structural, orbital and spin-driven nematic) are very entangled  
no matter which drives the nematic instability.

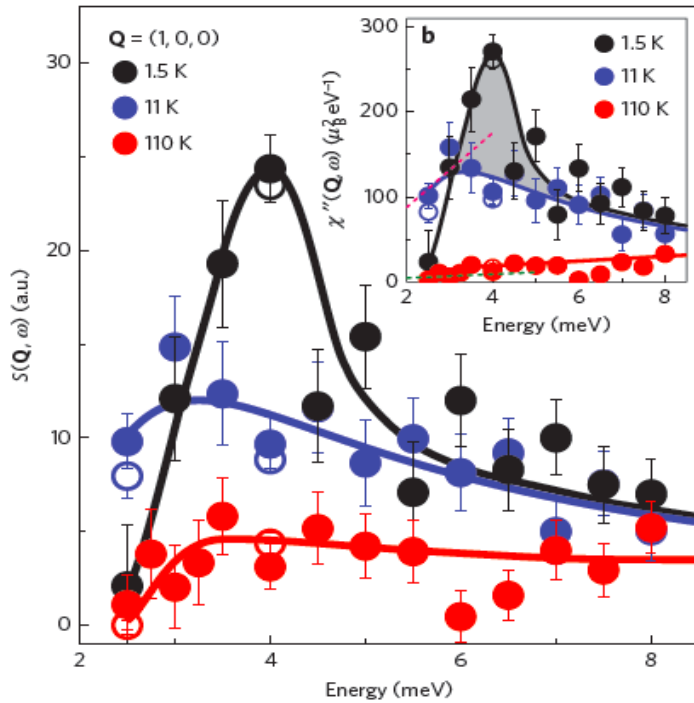
*What drives nematic order in iron-based superconductors?*

R.M. Fernandes et al. NATURE PHYSICS | VOL 10 | FEBRUARY 2014

*Enigmatic nematic*

J. C. Davis and P. J. Hirschfeld NATURE PHYSICS | ADVANCE ONLINE PUBLICATION 2014

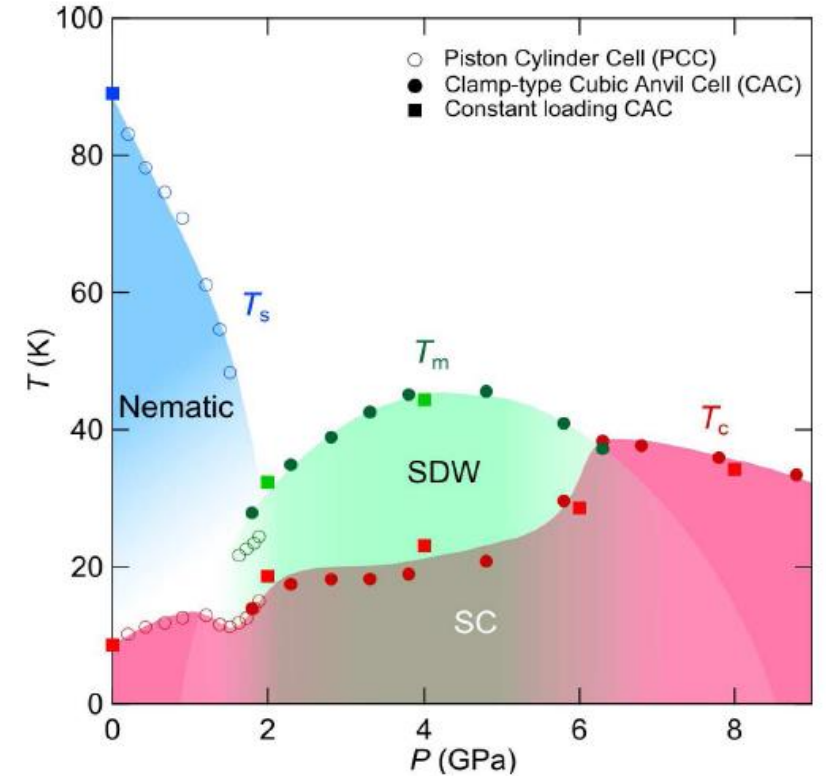
# THE CASE OF FESE: NEMATIC PHASE NOT FOLLOWED BY THE MAGNETIC ONE



Q. Wang et al. Nat. Mat. (2015)

Sizeable SDW fluctuations  
but NOT magnetic long  
range ordered phase

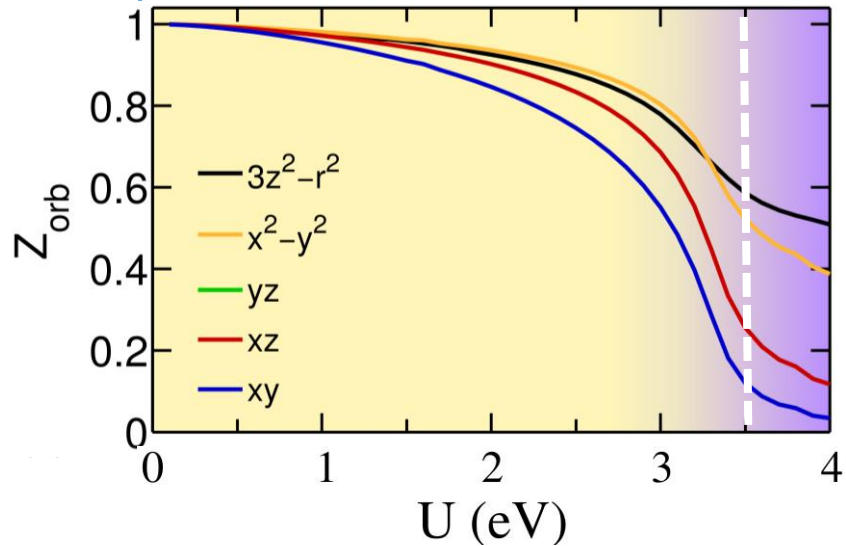
Sun et al Nat. Commun. 7 (2016)



*Is the charge degree of freedom the driver?*

*Local correlations can induce a nematic phase transition?*

# CORRELATIONS IN NEMATIC PHASE OF IBS



From ARPES, Quantum oscillations,  
X ray FeSe ~  
 $U = 3.5$  eV and  $J_H/U = 0.20$

Compute the Response of the system to **orbital perturbations modulated in k-space**:

$$\delta H_{A_{1g}/B_{1g}}^m = \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) h_m$$

Orbital Nematic Parameter:

$$\Delta_m = -\langle \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) \rangle$$

Linear response:

$$\chi_m = \frac{\delta \Delta_m}{\delta h_m}$$



# CORRELATIONS IN NEMATIC PHASE OF IBS

$$\delta H_{A_{1g}/B_{1g}}^m = \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) h_m$$

$$\Delta_m = -\langle \sum_{\mathbf{k}} (n_{xz}(\mathbf{k}) \pm n_{yz}(\mathbf{k})) f_m(\mathbf{k}) \rangle$$

**Onsite ferro-orbital**

$$h_{OFO} = \delta\epsilon \quad f_{OFO}(\mathbf{k}) = 1$$

$$\begin{array}{c} \epsilon_{zx} \\ \epsilon_{yz} \end{array} \begin{array}{c} \text{---} \\ \text{---} \end{array} \updownarrow \delta\epsilon$$

3 Orbital Orders considered in literature:

**Sign-change orbital order**

$$h_{SCO} = \delta t' \quad f_{SCO}(\mathbf{k}) = \cos k_x \cos k_y$$

Lift the degeneracy of the second neighbor hopping

**d-wave bond order**

$$h_{DBO} = \delta t \quad f_{DBO}(\mathbf{k}) = (\cos kx - \cos ky)/2.$$

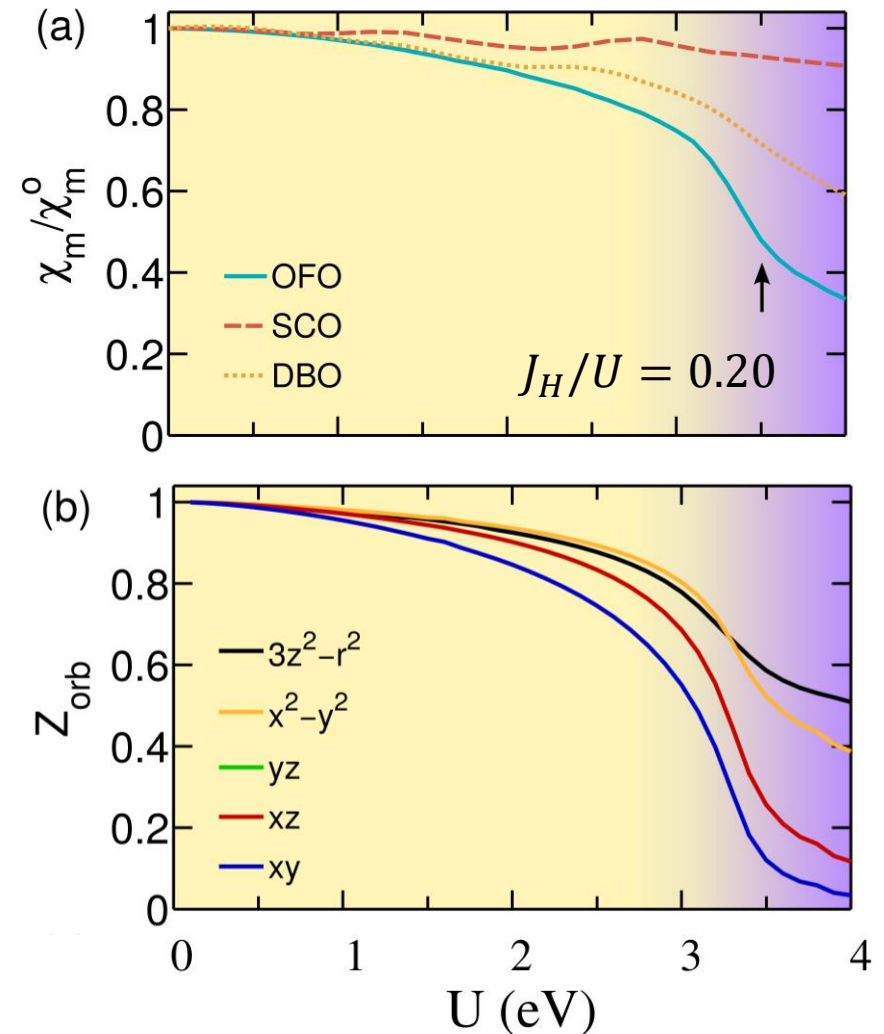
Lift the degeneracy of the nn hopping

# ORBITAL RESPONSE FUNCTIONS

No divergence = no phase transition

Hund's coupling strongly suppresses OFO order. SCO order is independent by U

*Suppression in correspondence of the entrance in the Hund Metal region.*

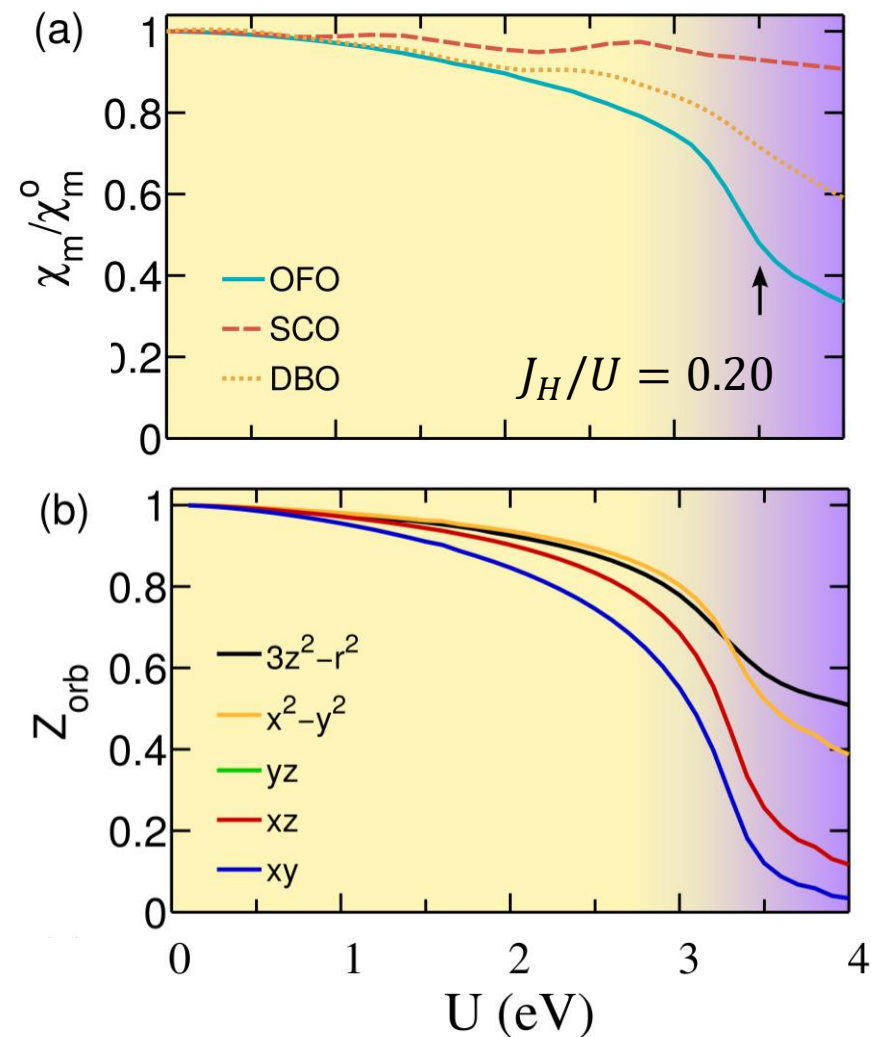
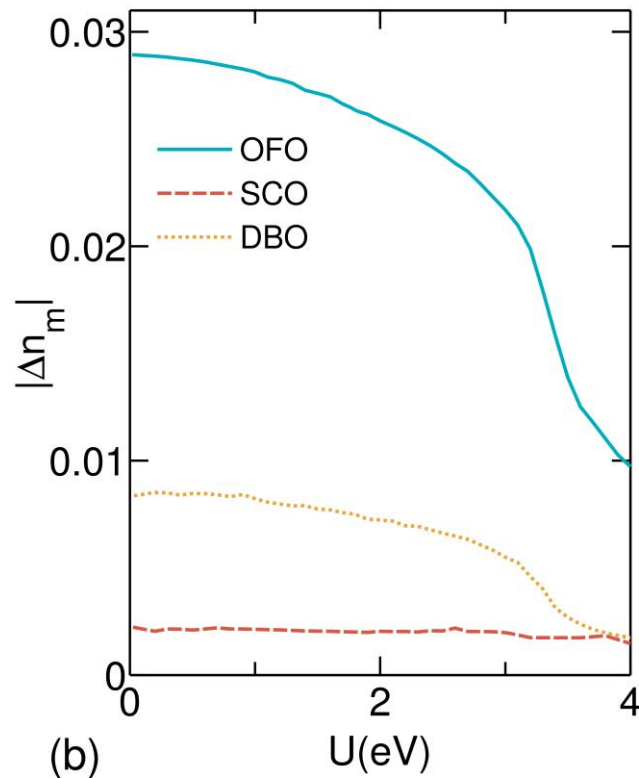


# ORBITAL RESPONSE FUNCTIONS

Sign-changing orbital order

small occupation imbalance  
between  $zx$  and  $yz$  orbitals

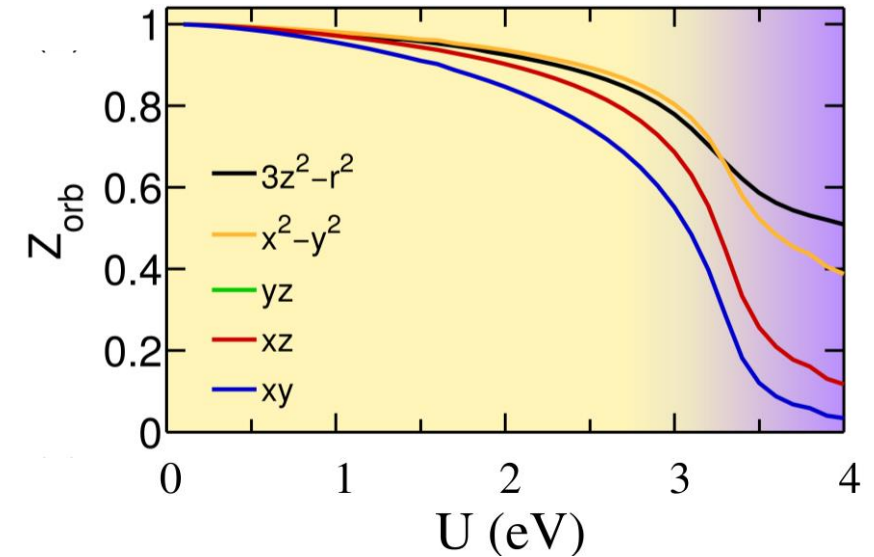
not suppressed by Hund's  
coupling!



# ENHANCED NEMATICITY & HUND METAL PHASE

New route to nematicity:  
anisotropy in the orbital mass.

$$\chi_Z^m(U) = \frac{\delta(Z_{zx} - Z_{yz})}{\delta h_m}$$



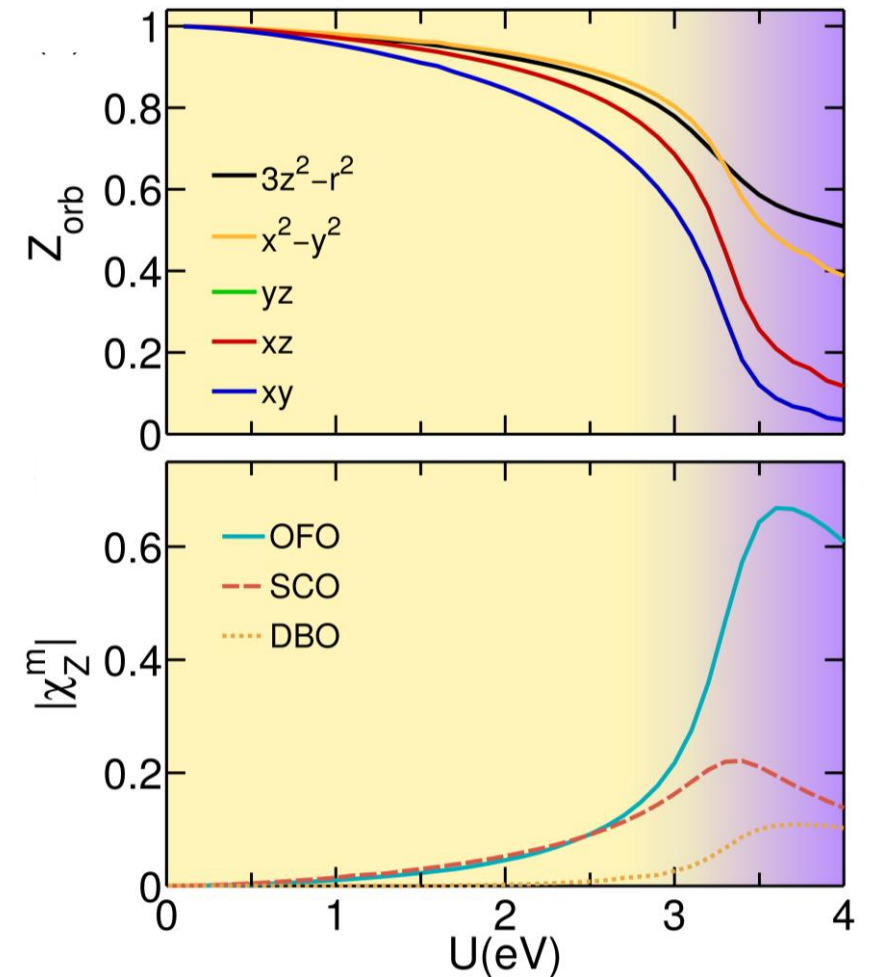
# ENHANCED NEMATICITY & HUND METAL PHASE

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$$\chi_Z^m(U) = \frac{\delta(Z_{zx} - Z_{yz})}{\delta h_m}$$

Anisotropy in the orbital mass is induced by  
the orbital order perturbation.

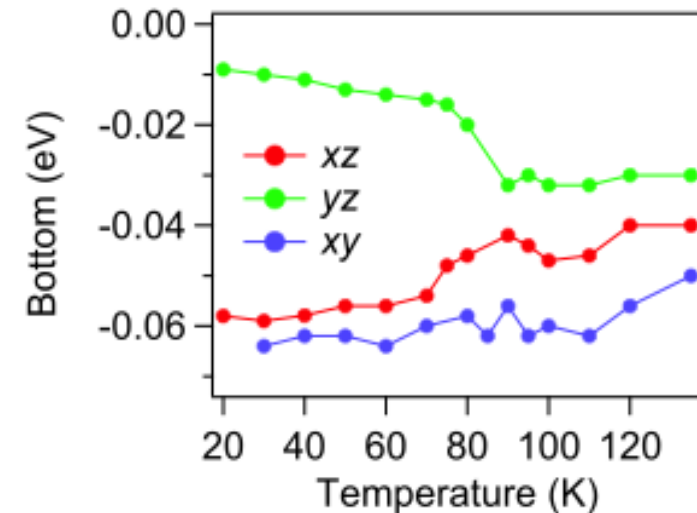
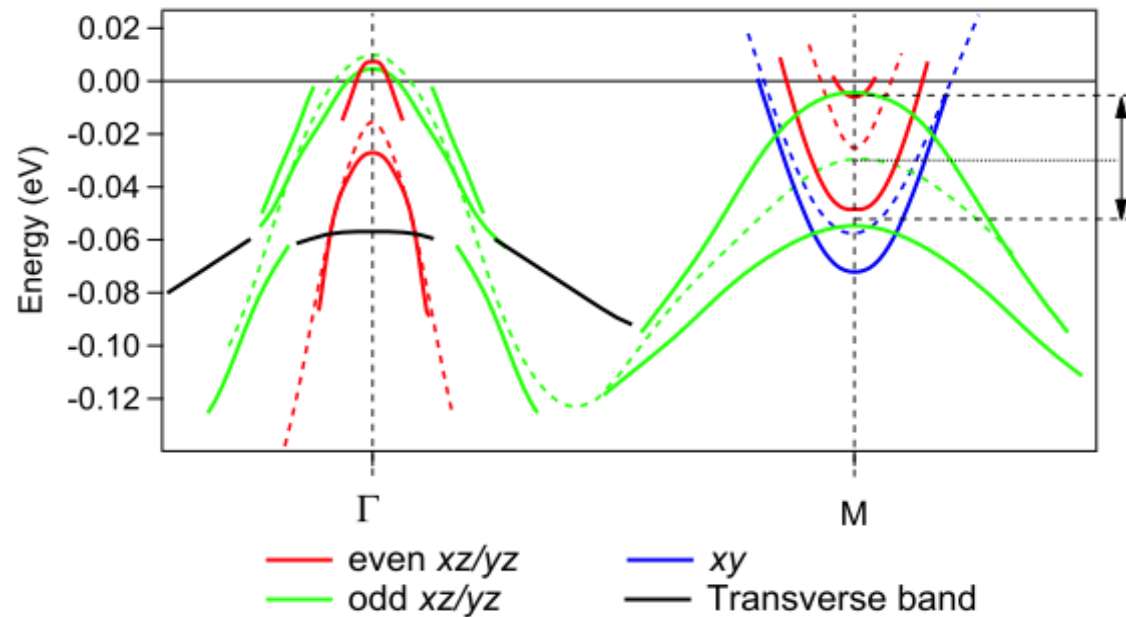
*Enhanced response at the entrance of the Hund  
Metal.*



# EFFECT ON THE BAND STRUCTURE

In the PARAMAGNETIC state  $xz$  and  $yz$  are degenerate = NO splitting at the symmetry points

In the NEMATIC state finite splitting appears between  $xz$  and  $yz$  bands at the symmetry points.



# EFFECT ON THE BAND STRUCTURE

In the PARAMAGNETIC state  $zx$  and  $yz$  are degenerate = NO splitting at the symmetry points

In the NEMATIC state finite splitting appears between  $zx$  and  $yz$  bands at the symmetry points.

Given an orbital perturbation the naive splitting expected at the  $\Gamma$  and  $M$  point are:

$$Sp_{\Gamma}^{OFO}(U=0) = 2\delta\epsilon$$

$$Sp_{\Gamma}^{SCO}(U=0) = 2\delta t'$$

$$Sp_{\Gamma}^{DBO}(U=0) = 0$$

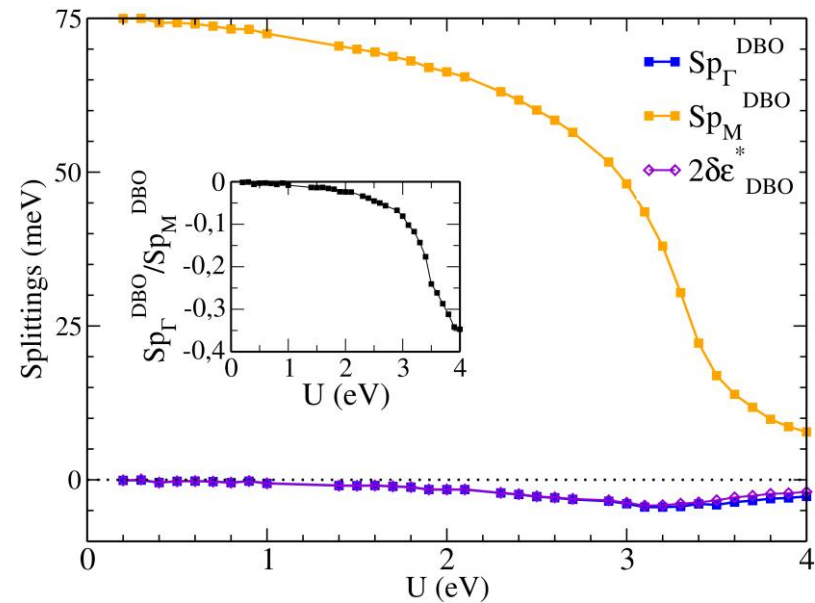
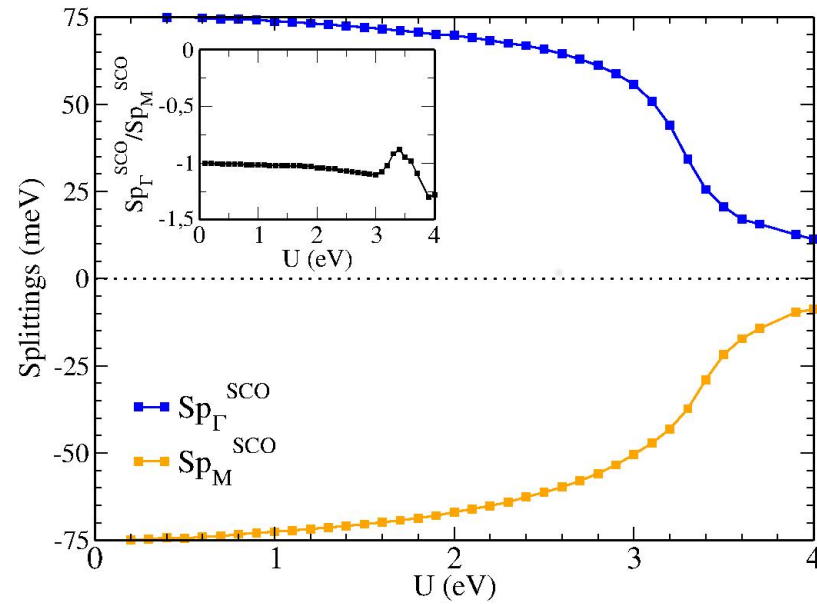
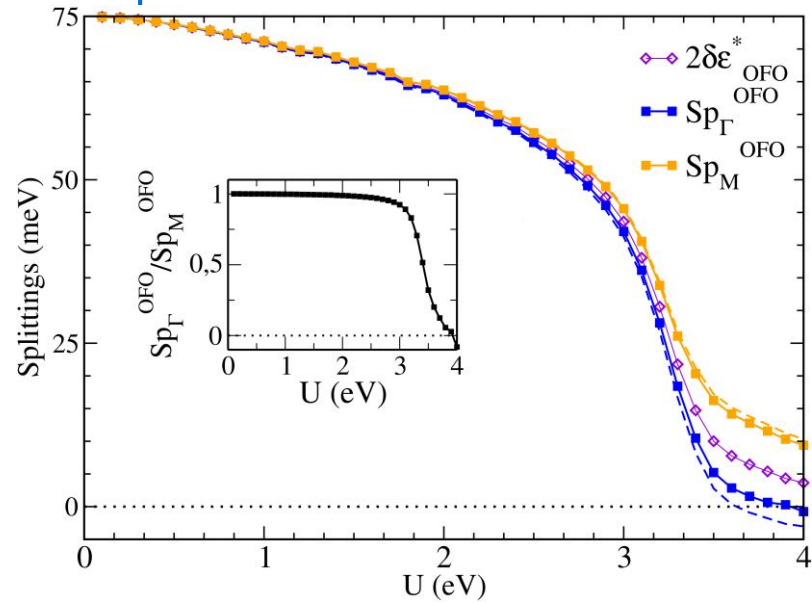
$$Sp_M^{OFO}(U=0) = 2\delta\epsilon$$

$$Sp_M^{SCO}(U=0) = -2\delta t'$$

$$Sp_M^{DBO}(U=0) = 2\delta t \quad (!)$$

Interactions renormalize the band structure (via  $Z$   $xz/yz$  anisotropy) and can modify the bare splitting

# EFFECT ON THE BAND STRUCTURE



*Local Correlations modify the orbital splitting:  
Induce  $k$ -dependence, drive sign change ...*



# CONCLUSIONS: LOCAL CORRELATIONS AND NEMATICITY

- ✓ Correlations constrain possible orbital orders

The onsite ferro-orbital ordering would be strongly suppressed by Hund's, while a sign-changing orbital order gives small occupation imbalance between  $z_x$  and  $z_y$  orbitals and is not suppressed by Hund's coupling.

- ✓ Hund's coupling induces anisotropy in the correlation strength of  $z_x$  and  $z_y$  orbitals

This anisotropy affects the renormalization of the band structure, leading to distinctive signatures in different experimental probes including ARPES.

- ✓ Hund's physics modifies the magnitude of these splittings, their relative value and even their sign.

# CONCLUSIONS: HUND'S PHYSICS IN IBS

- ✓ No evidences of nematic transition in the orbital channel

Nematicity in the **charge channel** assisted by spin fluctuations

Chubukov et al. arxiv 1602.05503

SCO order parameter

Nematicity **driven by** other degree of freedom  
e.g. **spin-fluctuations**

Fanfarillo et al. arxiv 1605.02482

Sign change orbital polarization from  
orbital selective spin fluctuating

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